

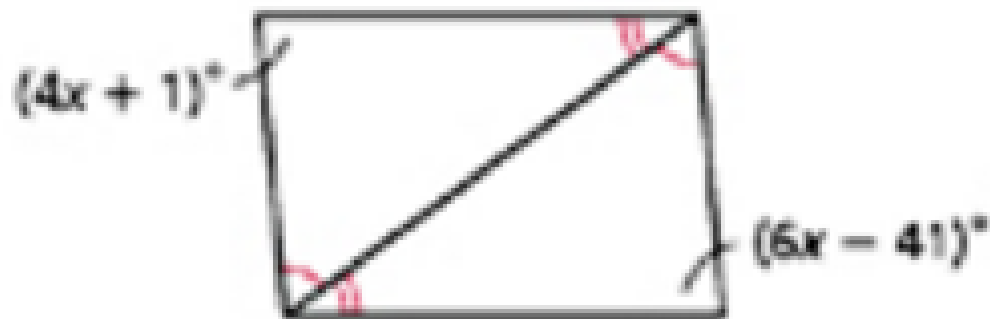
# 4-8 Isosceles and Equilateral Triangles

## Bellwork

1.



2.



## *Objectives*

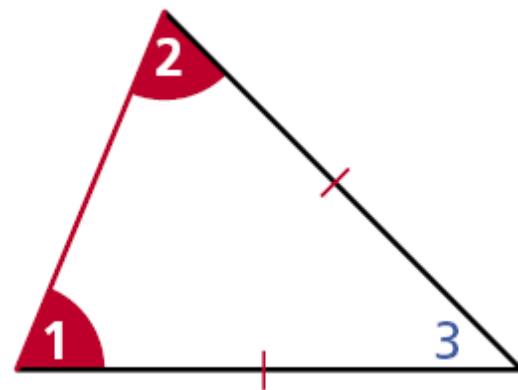
Properties of isosceles and equilateral triangles.

## 4-8 Isosceles and Equilateral Triangles

Recall that an isosceles triangle has at least two congruent sides. The congruent sides are called the **legs**. The **vertex angle** is the angle formed by the legs. The side opposite the vertex angle is called the **base**, and the **base angles** are the two angles that have the base as a side.

$\angle 3$  is the vertex angle.

$\angle 1$  and  $\angle 2$  are the base angles.

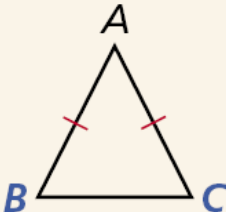
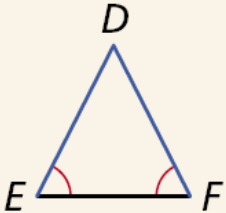


## 4-8

## Isosceles and Equilateral Triangles

## Theorems

## Isosceles Triangle

THEOREM	HYPOTHESIS	CONCLUSION
<p><b>4-8-1 Isosceles Triangle Theorem</b> If two sides of a triangle are congruent, then the angles opposite the sides are congruent.</p>		$\angle B \cong \angle C$
<p><b>4-8-2 Converse of Isosceles Triangle Theorem</b> If two angles of a triangle are congruent, then the sides opposite those angles are congruent.</p>		$\overline{DE} \cong \overline{DF}$

# 4-8 Isosceles and Equilateral Triangles

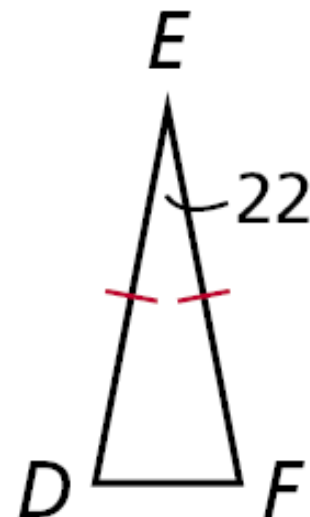
## Reading Math

The Isosceles Triangle Theorem is sometimes stated as “Base angles of an isosceles triangle are congruent.”

# 4-8 Isosceles and Equilateral Triangles

## Example 2A: Finding the Measure of an Angle

Find  $m\angle F$ .



$$m\angle F = m\angle D = x^\circ \quad \text{Isosc. } \Delta \text{ Thm.}$$

$$m\angle F + m\angle D + m\angle A = 180 \quad \Delta \text{ Sum Thm.}$$

$$x + x + 22 = 180 \quad \text{Substitute the given values.}$$

$$2x = 158 \quad \text{Simplify and subtract 22 from both sides.}$$

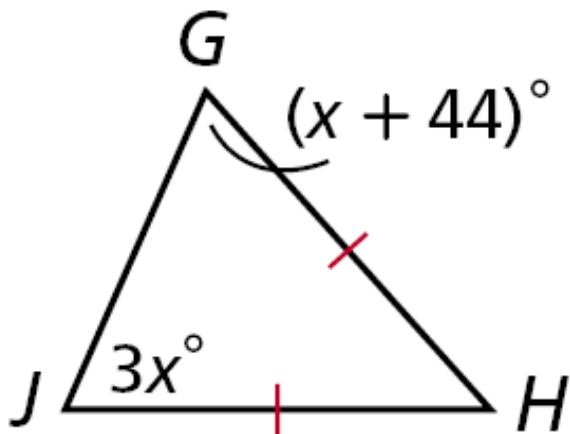
$$x = 79^\circ \quad \text{Divide both sides by 2.}$$

Thus  $m\angle F = 79^\circ$

# 4-8 Isosceles and Equilateral Triangles

## Example 2B: Finding the Measure of an Angle

Find  $m\angle G$ .



$$m\angle J = m\angle G \quad \text{Isosc. } \Delta \text{ Thm.}$$

$$(x + 44)^\circ = 3x^\circ$$

*Substitute the given values.*

$$44 = 2x$$

*Simplify  $x$  from both sides.*

$$x = 22^\circ$$

*Divide both sides by 2.*

$$\text{Thus } m\angle G = 22^\circ + 44^\circ = 66^\circ.$$

## 4-8

## Isosceles and Equilateral Triangles

## Check It Out! Example 2A

Find  $m\angle H$ .

$$m\angle H = m\angle G = x^\circ \quad \text{Isosc. } \Delta \text{ Thm.}$$

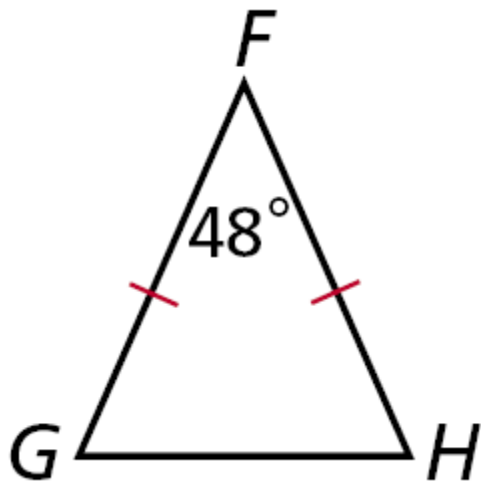
$$m\angle H + m\angle G + m\angle F = 180 \quad \Delta \text{ Sum Thm.}$$

$$x + x + 48 = 180 \quad \text{Substitute the given values.}$$

$$2x = 132 \quad \text{Simplify and subtract 48 from both sides.}$$

$$x = 66^\circ \quad \text{Divide both sides by 2.}$$

$$\text{Thus } m\angle H = 66^\circ$$





# 4-8 Isosceles and Equilateral Triangles

## Check It Out! Example 2B

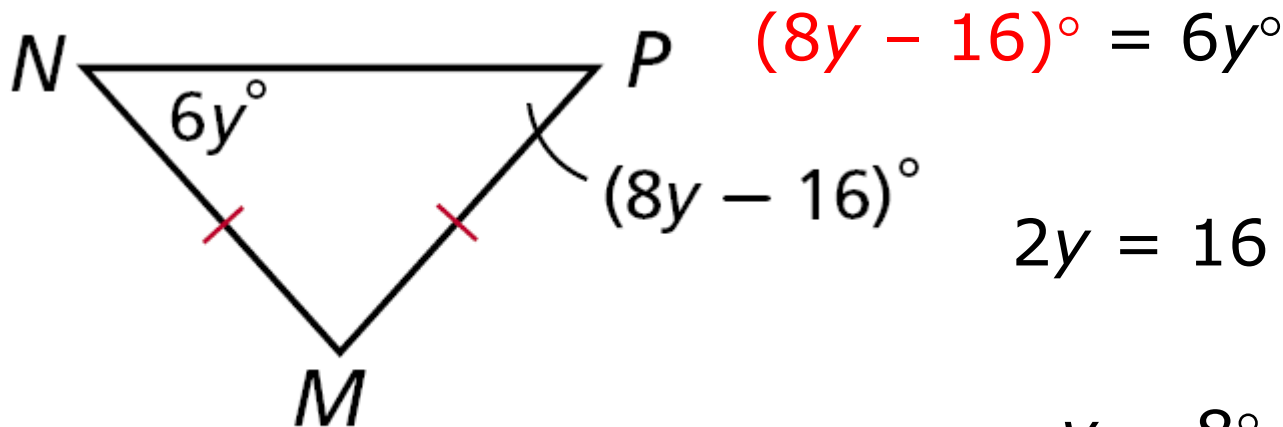
Find  $m\angle N$ .

$$m\angle P = m\angle N \quad \text{Isosc. } \Delta \text{ Thm.}$$

*Substitute the given values.*

*Subtract  $6y$  and add 16 to both sides.*

*Divide both sides by 2.*



$$\text{Thus } m\angle N = 6(8) = 48^\circ.$$

# 4-8 Isosceles and Equilateral Triangles

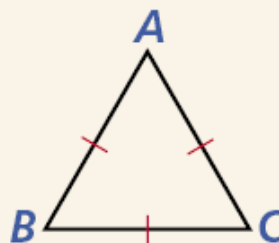
## Corollary 4-8-3 Equilateral Triangle

### COROLLARY

If a triangle is equilateral, then it is equiangular.  
(equilateral  $\triangle \rightarrow$  equiangular  $\triangle$ )



### HYPOTHESIS



### CONCLUSION

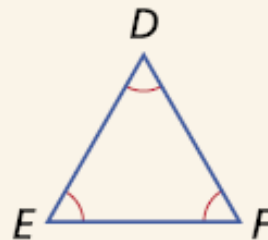
$$\angle A \cong \angle B \cong \angle C$$

## Corollary 4-8-4 Equiangular Triangle

### COROLLARY

If a triangle is equiangular, then it is equilateral.  
(equiangular  $\triangle \rightarrow$  equilateral  $\triangle$ )

### HYPOTHESIS



### CONCLUSION

$$\overline{DE} \cong \overline{DF} \cong \overline{EF}$$

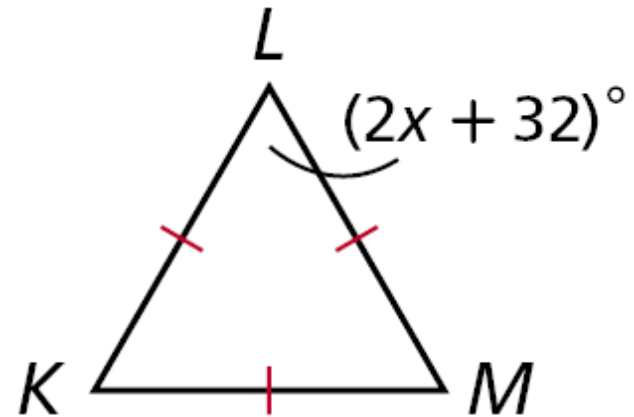
# 4-8 Isosceles and Equilateral Triangles

## Example 3A: Using Properties of Equilateral Triangles

Find the value of  $x$ .

$\triangle LKM$  is equilateral.

*Equilateral  $\triangle \rightarrow$  equiangular  $\triangle$*



$$(2x + 32)^\circ = 60^\circ \quad \text{The measure of each } \angle \text{ of an equiangular } \triangle \text{ is } 60^\circ.$$

$$2x = 28 \quad \text{Subtract 32 both sides.}$$

$$x = 14 \quad \text{Divide both sides by 2.}$$

# 4-8 Isosceles and Equilateral Triangles

## Example 3B: Using Properties of Equilateral Triangles

**Find the value of  $y$ .**

$\triangle NPO$  is equiangular.

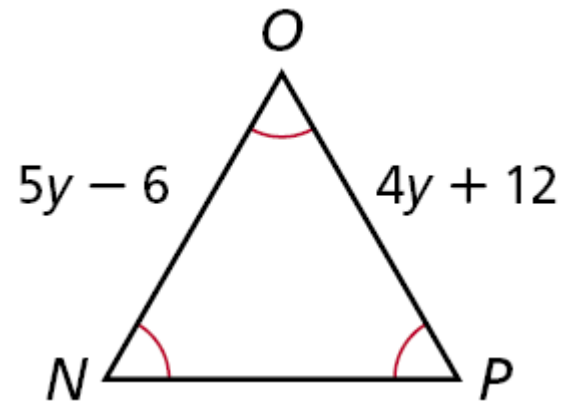
*Equiangular  $\triangle \rightarrow$  equilateral  $\triangle$*

$$5y - 6 = 4y + 12$$

$$y = 18$$

*Definition of equilateral  $\triangle$ .*

*Subtract  $4y$  and add 6 to both sides.*



# 4-8 Isosceles and Equilateral Triangles

## Check It Out! Example 3

Find the value of  $JL$ .

$\triangle JKL$  is equiangular.

*Equiangular  $\triangle \rightarrow$  equilateral  $\triangle$*

$$4t - 8 = 2t + 1$$

*Definition of equilateral  $\triangle$ .*

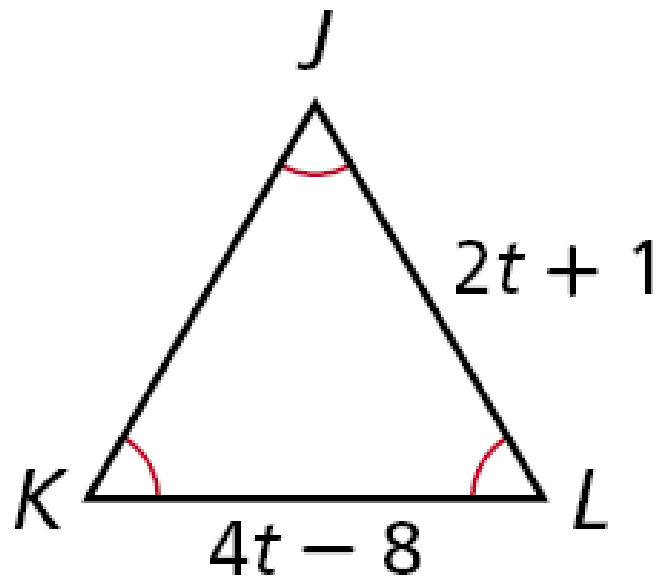
$$2t = 9$$

*Subtract  $4y$  and add 6 to both sides.*

$$t = 4.5$$

*Divide both sides by 2.*

$$\text{Thus } JL = 2(4.5) + 1 = 10.$$



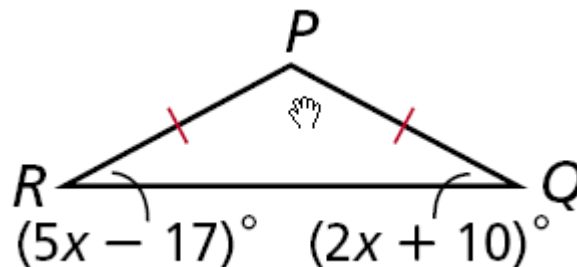
# 4-8 Isosceles and Equilateral Triangles

## Lesson Quiz: Part I

Find each angle measure.

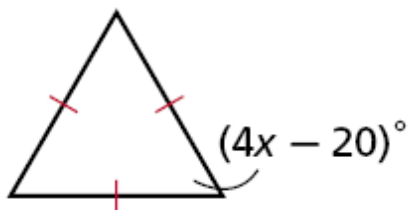
1.  $m\angle R$   $28^\circ$

2.  $m\angle P$   $124^\circ$



Find each value.

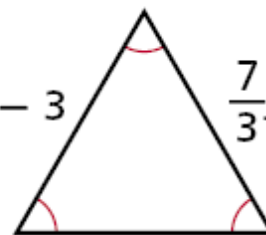
3.  $x$



$20$

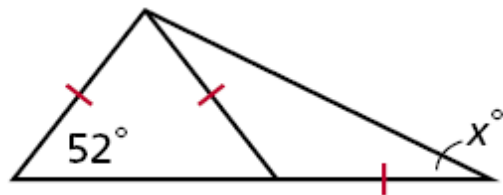
4.  $y$

$\frac{2}{3}y - 3$



$\frac{7}{3}y - 13$   $6$

5.  $x$



$26^\circ$

## Lesson Quiz: Part II

6. The vertex angle of an isosceles triangle measures  $(a + 15)^\circ$ , and one of the base angles measures  $7a^\circ$ . Find  $a$  and each angle measure.

$$a = 11; 26^\circ; 77^\circ; 77^\circ$$

# **4-8** Isosceles and Equilateral Triangles

## HOMEWORK

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